## **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**International General Certificate of Secondary Education** 

## MARK SCHEME for the May/June 2014 series

## 0606 ADDITIONAL MATHEMATICS

**0606/22** Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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1	rationalise the denominator to get $\frac{(2+\sqrt{5})^2(\sqrt{5}+1)}{5-1}$ or better squaring to get	M1	or squaring to get $\frac{\left(4+4\sqrt{5}+5\right)}{\sqrt{5}-1}$ or better
	$\frac{\left(4+4\sqrt{5}+5\right)\left(\sqrt{5}+1\right)}{their4}$ or better	M1	or rationalising the denominator to get $\frac{their(9+4\sqrt{5})(\sqrt{5}+1)}{5-1}$ or better
	$\frac{29}{4} + \frac{13}{4}\sqrt{5} \text{ oe isw}$	A1 + A1	correct simplification
			Allow $\frac{29+13\sqrt{5}}{4}$ etc.
2	Correctly eliminate <i>y</i>	M1	$-kx + 2 = 2x^2 - 9x + 4 \text{ oe}$
	$2x^2 + (k-9)x + 2[=0]$ oe	A1	allow even if $x$ terms not collected; condone = $y$ provided later work implies it should be 0
	Use $b^2 - 4ac$ oe	M1	must be applied to a 3 term quadratic expression containing $k$ as a coefficient; condone $< 0$ etc.
	Reach their $(k-9=\pm 4)$ or solves their $(k^2-18k+65)=0$	M1	condone $9-k=\pm 4$ ; condone an inequality at this stage
	k = 5 and 13 cao	A1	mark final answer, do not isw; <b>A0</b> if inequalities for final answers

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3 (i)	$3(-1)^3 - 14(-1)^2 - 7(-1) + d = 0$ with completion to $d = 10$	B1	at least $-3 - 14 + 7 + d = 0$ , d = 10; N.B. = 0 must be seen or implied by = $d$ or = $-d$ , may be seen in following step. or convincingly showing $3(-1)^3 - 14(-1)^2 - 7(-1) + 10 = 0$ ; at least $-3 - 14 + 7 + 10 = 0$ or correct synthetic division at least as far as $-1 \begin{bmatrix} 3 & -14 & -7 & 10 \\ -3 & 17 & -10 \\ \hline 3 & -17 & 10 \end{bmatrix}$	
(ii)	$3x^2 - 17x + 10$ isw or $a = 3$ , $b = -17$ , $c = 10$ isw	B2, 1, 0	-1 each error; must be seen or referenced in (ii) even if found in (i) or (iii)	
(iii)	(x+1)(x-5)(3x-2)	M1	for factorising quadratic <b>ft</b> correct; condone omission of $(x+1)$ or for <b>ft</b> correct use of formula or <b>ft</b> correct completing the square	
	$-1, 5, \frac{2}{3}$	A1	If <b>M0</b> then <b>SC1</b> for all three roots stated without working or verified/found by trials	

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4	(i)	$12\left(x - \frac{1}{4}\right)^2 + \frac{17}{4}$ isw	B3, 2, 1,0	one mark for each of $p$ , $q$ , $r$ correct in a correctly formatted expression;
				allow correct equivalent values;
				If <b>B0</b> then <b>SC2</b> for $12\left(x - \frac{1}{4}\right) + \frac{17}{4}$
				or
				SC1 for correct 3 values seen in incorrect format e.g.
				$12\left(x - \frac{1}{4}x\right) + \frac{17}{4} \text{ or }$
				$12\left(x^2 - \frac{1}{4}\right) + \frac{17}{4}$
				or for a correct completed square form of the original expression in a
				different but correct format. e.g. $3\left(2x - \frac{1}{2}\right)^2 + \frac{17}{4}$
	(ii)	their $\frac{4}{17}$ or their 0.235	B1ft	strict <b>ft</b> ; their $\frac{4}{17}$ must be a proper
				fraction or decimal rounded to 3sig figs or more or truncated to 4 figs or more
		their $x = \frac{1}{4}$ oe	B1ft	strict <b>ft</b> ; <i>x</i> must be correctly attributed
5	(i)	$1-20x+160x^2$	B2, 1, 0	-1 each error
				if <b>B0</b> then <b>M1</b> for 3 correct terms seen; may be unsimplified e.g. 1, $5(-4x)$ , $\frac{5\times4}{2}(-4x)^2$
	(ii)	a + (their - 20) = -23  soi	M1	condone sign errors only; must be <i>their</i> –20 from (i)
		a = -3	<b>A1</b>	validly obtained
		b + (their - 20)a + (their 160) = 222 soi	M1	condone sign errors only; must be <i>their</i> –20 and <i>their</i> 160 from (i) and <i>their a</i> if used
		b = 2	<b>A1</b>	validly obtained

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6 (a) (i)	1	B1	
(ii)	x = -1  or  -2	B1 + B1	as final answers
(b)	$\frac{\log_3 5}{\log_3 a}$ seen or implied	B1*	may be implied by $2\log_3 15 - \log_3 5$
	$2\log_3 15 = \log_3 15^2$ seen or implied	B1	
	$\log_3 15^2 - \log_3 5 = \log_3 \left(\frac{15^2}{5}\right)$	B1dep*	not from wrong working
	$\log_3 45$ cao	B1	must be 45 not e.g. $\frac{225}{5}$ ; with no wrong working seen
7 (i)	$x^4(3e^{3x}) + 4x^3e^{3x}$ isw	B1 + B1	each term of the <b>sum</b> correct; must be a sum of two terms
(ii)	$x^{4}(3e^{3x}) + 4x^{3}e^{3x} \text{ isw}$ $\frac{1}{2 + \cos x} \times (-\sin x) \text{ isw}$	B2	or <b>B1</b> for $\frac{1}{2 + \cos x} \times (k \pm \sin x)$ and $k$ a constant
(iii)	$\frac{\mathrm{d}}{\mathrm{d}x}(\sin x) = \cos x \ \mathrm{soi}$	B1	
	$\frac{\mathrm{d}}{\mathrm{d}x}\left(1+\sqrt{x}\right) = \frac{1}{2}x^{-\frac{1}{2}} \text{ soi}$	B1	
	$\frac{\left(1+\sqrt{x}\right)their\cos x - \left(their\frac{1}{2}x^{-\frac{1}{2}}\right)\sin x}{\left(1+\sqrt{x}\right)^{2}}$ isw	B1ft	for correct form of quotient rule <b>ft</b> their $\cos x$ and their $\frac{1}{2}x^{-\frac{1}{2}}$ ;
			allow correct use of product and chain rules to obtain $\sin x \left( -\left(1 + \sqrt{x}\right)^{-2} \times \frac{1}{2} x^{\frac{1}{2}} \right) + \cos x \left(1 + \sqrt{x}\right)^{-1} \text{ oe}$

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8	Substitution of either $x - 5$ or $y + 5$ into equation of curve and brackets expanded	M1	condone one sign error in either equation of curve or expansion of brackets; condone omission of $= 0$ , BUT $x - 5$ or $y + 5$ must be correct
	$2x^2 - 8x - 10[= 0]$ or $2y^2 + 12y[= 0]$ obtained	A1	
	Solving their quadratic	M1	dep on a valid substitution attempt
	(-1, -6) oe and $(5, 0)$ oe isw	A1*+A1*	or A1 for correct pair of $x$ coordinates or correct pair of $y$ coordinates
	$\sqrt{72}$ or $6\sqrt{2}$ cao isw	B1dep*	
9 (i)	$[y=]\frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} (+c)$ oe	B2	or <b>B1</b> for $(2x+1)^{\frac{1}{2}+1}$
	$10 = \frac{2}{6} (2(4) + 1)^{\frac{3}{2}} + c \text{ oe}$	M1	for valid attempt to find $c$ ; condone slips e.g. omission of power or sign error
	$y = \frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + c$ seen and $c = 1$ or	A1	must have $y =$ ; condone $f(x) =$
	$y = \frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + 1$ isw		
(ii)	2		
	$\int \left(\frac{1}{3}(2x+1)^{\frac{3}{2}}+1\right) dx = \frac{1}{15}(2x+1)^{\frac{5}{2}}+x(+const)$	B1 + B1	<b>B1</b> for $(2x+1)^{\frac{3}{2}+1}$ ,
			<b>B1</b> for $\frac{1}{15}(2x+1)^{\frac{5}{2}}$
	$\left[ \frac{1}{15} (2x+1)^{\frac{5}{2}} + x \right]_{0}^{1.5} =$	B1ft	<b>B1 ft</b> their c from (i) provided $c \neq 0$
	$\left[\frac{1}{15}(2x+1)^{\frac{5}{2}} + x\right]_{0}^{1.5} = \left[\frac{1}{15}(2(1.5)+1)^{\frac{5}{2}} + (1.5)\right] - \left[\frac{1}{15}(2(0)+1)^{\frac{5}{2}} + 0\right]$	M1	for a genuine attempt to find $F(1.5)$ – $F(0)$ in an attempt to integrate their $y$ ; if their $F(0)$ is 0 must see at least their $F(1.5)$ – 0; condone + $c$ as long as their $c$ is <b>not</b> numerical.
	$\frac{107}{30}$ oe isw	A1	if decimal 3.57 or more accurate e.g. 3.566

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10 (i)	Taking logs of both sides	M1	any base; must be an explicitly correct statement
	$\log y = \log A + x \log b$	A1	correct form; any base; no recovery from incorrect method steps
(ii)	b: awrt 3 to one sf isw or awrt 4 to one sf isw	B2	or <b>M1</b> for $b = e^{their \text{ gradient}}$ soi; their gradient must be correctly evaluated as rise/run
	A: awrt 0.5 to one sf	B2	or <b>B1</b> for $A = e^{-0.6}$
			or <b>SC1</b> for $A = e^{-0.3} = 0.7$ (giving an awrt 0.7)
(iii)	Evidence of graph used at $\ln y = 5.4$ soi	M1	or $\frac{220}{their 0.5} = (their 4)^x$
			or $5.39 = their(1.4)x + their -0.6$
			or $\ln(220) = x \ln(their 4) + \ln(their 0.5)$
	awrt 4.4 to two sf	<b>A1</b>	

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11 (i)	$f(x) > 3 \text{ or } [f(x) \in ](3, \infty)$	B1	condone $y > 3$
(ii)	$x + 1 = 2^{y}$ $f^{-1}(x) = \log_{2}(x+1)$	M1 A1	or $y+1=2^x$ mark final answer or $\log_2(y+1)=x$ and $f^{-1}(x) = \log_2(x+1)$ or for $f^{-1}(x) = \frac{\log(x+1)}{\log 2}$ (any base for this form)
	Domain $x > 3$	B1ft	ft their range of f provided mathematically valid inequality or interval
	Range $f^{-1}(x) > 2$	B1	condone $f(x) > 2$ or $y > 2$
(iii)	$2^{x}(2^{x}-1)$ oe isw	B1	e.g. $(2^{x} - 1)^{2} + (2x - 1)$ or $2^{2x} - 2 \times 2^{x} + 1 + 2^{x} - 1$
	$2^{x}(2^{x}-1)=0$ leading to $2^{x}=0$ , impossible oe	B1	or $2^x = 0$ which is outside domain of gf
	$2^x = 1 \Rightarrow x = 0$	M1	or $2^{x}(2^{x}-1)=2^{2x}-2^{x}=0$ $[2^{2x}=2^{x}] \Rightarrow x=0$
	0 is not in the domain (and so $gf(x) = 0$ has no solutions)	<b>A1</b>	[ ] <del>-                               </del>

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12 (i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - 18x + 24$	B1	
	Solving their $3x^2 - 18x + 24 \ge 0$ by factorising or quadratic formula or completing the square	M1	attempt at differentiation resulting in quadratic expression with two terms correct; allow = or $\leq$ or $<$ or $>$ or $\geq$ 0 omitted here.
	Critical values 2 and 4 $x \le 2, x \ge 4$	A1 A1	A0 if spurious attempt to combine; mark final answer
(ii)	Evaluating their $\frac{dy}{dx}$ at $x = 3$	M1	
	Use of $m_1 m_2 = -1$ to get $m_{normal} = -\frac{1}{their(-3)}$	M1	must be explicit statement of gradient of normal; may be seen in equation
	y = 18 soi	B1	
	$y - their 18 = \left(their \frac{1}{3}\right)(x - 3)$ or		
	$y = their \frac{1}{3}x + c$ and $c = their 17$ isw	A1ft	<b>ft</b> their m provided a genuine attempt at $m_{normal}$ ; no <b>ft</b> if $m = their \ m_{tangent}$
	P(0, 17) cao	B1	